

# Hybrid AO's and polyatomic MO's

CH101 Fall 2015  
Boston University



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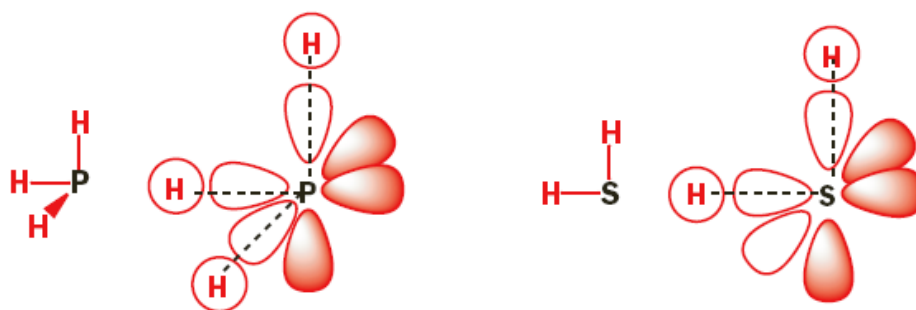
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**Hybridized AO's**  
account for central atom  
**electron-pair geometry**

# Central atom AO mixing: Hybrid AO's

**Unmixed** AO's have the **wrong** central atom **geometry**

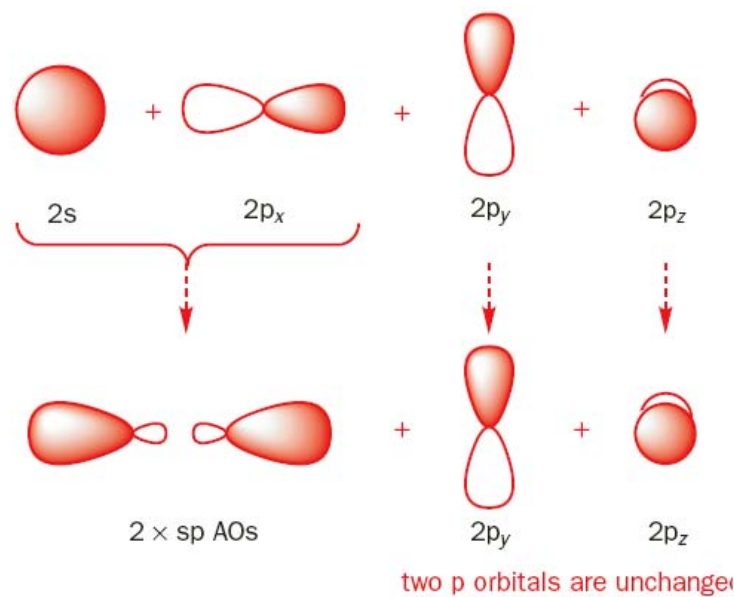


the  $90^\circ$  angles in  $\text{PH}_3$  and  $\text{H}_2\text{S}$  come from the overlap of the hydrogen 1s AO with the p AO of the phosphorus or sulfur

# An s and a p AO make two **sp hybrid** AO's

180° angle, for SN = 2

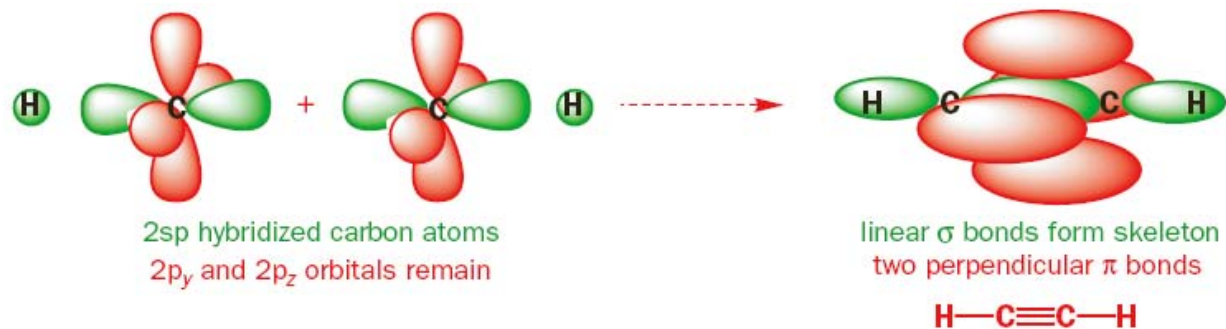
Two p's are unchanged on each atom



# sp hybrids account for **linear geometry**

180° angle, for SN = 2

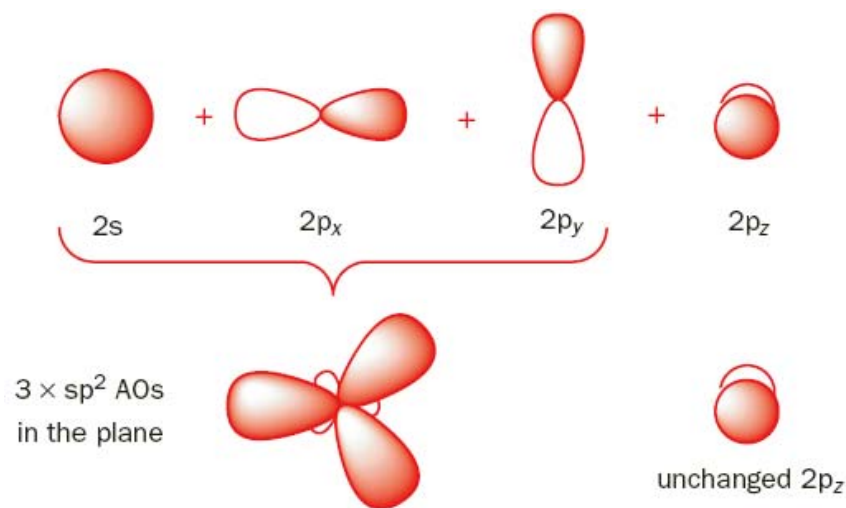
Two p's are unchanged on each atom



An s and two p AO's make  
three **sp<sup>2</sup> hybrid** AO's

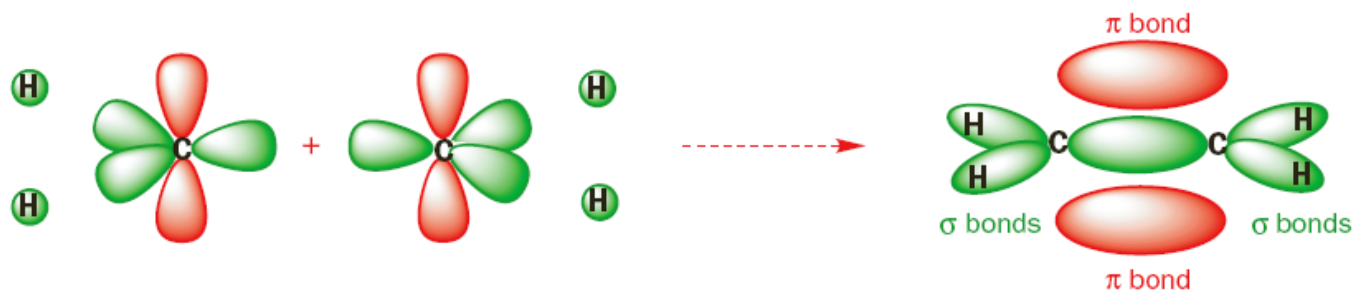
120° angle, for SN = 3

One p is unchanged on each atom



# $sp^2$ hybrids account for **trigonal planar geometry**

120° angle, for SN = 3  
One p is unchanged on each atom

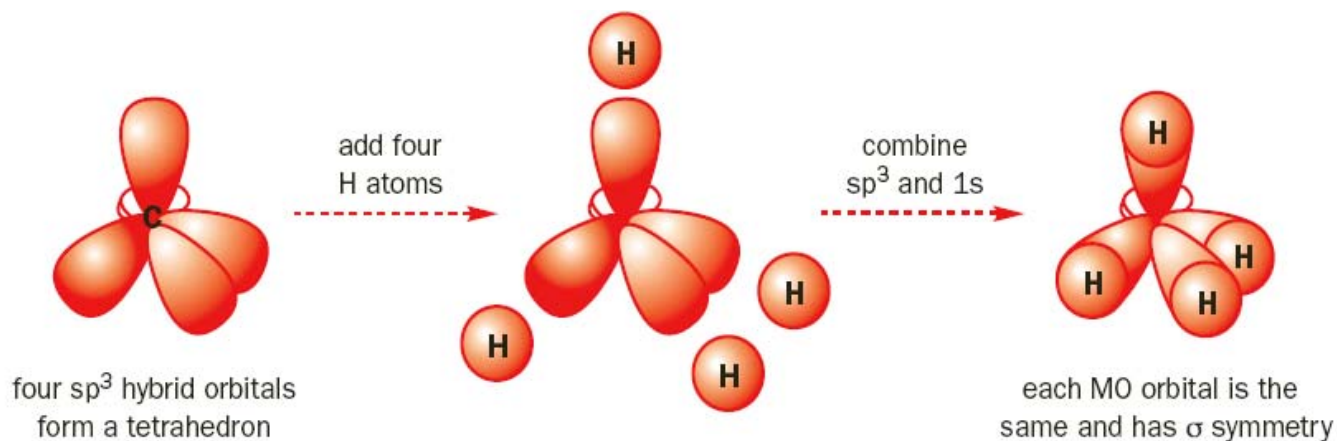




An s and three p AO's make  
four  **$sp^3$  hybrid** AO's

109° angle, for SN = 4

$sp^3$  hybrids account for **tetrahedral geometry**



# Which hybridization to use?

**steric number** → **electron-pair geometry** → hybridization  
 steric number = **attached atoms** + **lone pairs**

	steric number	electron-pair geometry	hybridization	molecular geometry
H <sub>2</sub> O	4	tetrahedral	sp <sup>3</sup>	bent at 109°
NH <sub>3</sub>	4	tetrahedral	sp <sup>3</sup>	trigonal pyramidal
CH <sub>4</sub>	4	tetrahedral	sp <sup>3</sup>	tetrahedral
SO <sub>2</sub>	3	trigonal planar	sp <sup>2</sup>	bent at 120°
BH <sub>3</sub>	3	trigonal planar	sp <sup>2</sup>	trigonal planar
CO <sub>2</sub>	2	linear	sp	linear at 180°

# Examples

$\text{CO}_2$ , carbon dioxide

$\text{H}_2\text{CO}$ , formaldehyde

$\text{HCO}_2^-$ , formate

$\text{SO}_2$ , sulfur dioxide

# Polyatomic MO recipe

## Overview

- **$\sigma$  framework** of **single bonds and lone pairs**
- **$\pi$  framework** of **additional bond pairs**
- **$\pi$  framework** can be **delocalized** (spread) over more than two atoms.

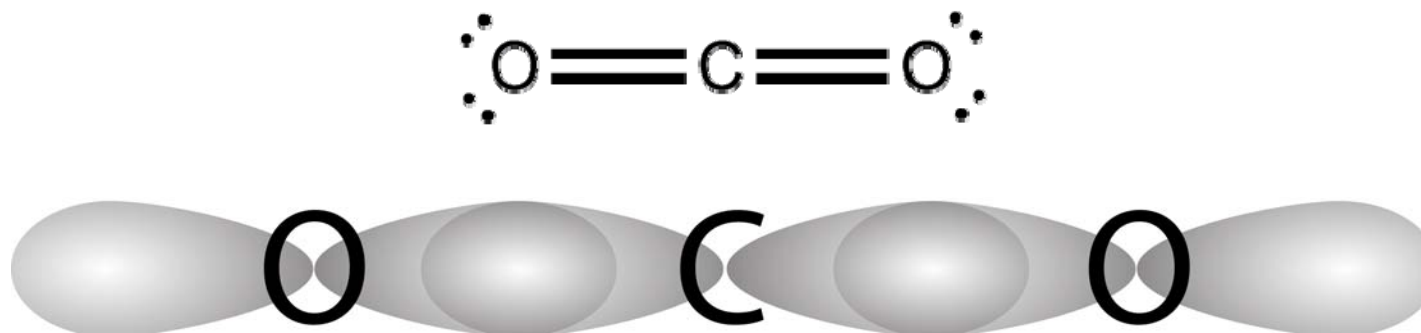
# Polyatomic MO recipe

1. Use the Lewis structure to get
  - the **number of electron pairs**
  - make **hybrid AO's** on each atom (except H)
2. Sketch the  **$\sigma$  framework** and **place pairs**
  - in each **bonding  $\sigma$  MO**
  - in each **nonbonding hybrid AO**
3. Sketch the  **$\pi$  framework MO's**,
  - mark as ***bonding, nonbonding, antibonding***
  - place **remaining pairs** (Auf Bau)
  - get the  **$\pi$  bond order**

## $\sigma$ framework recipe

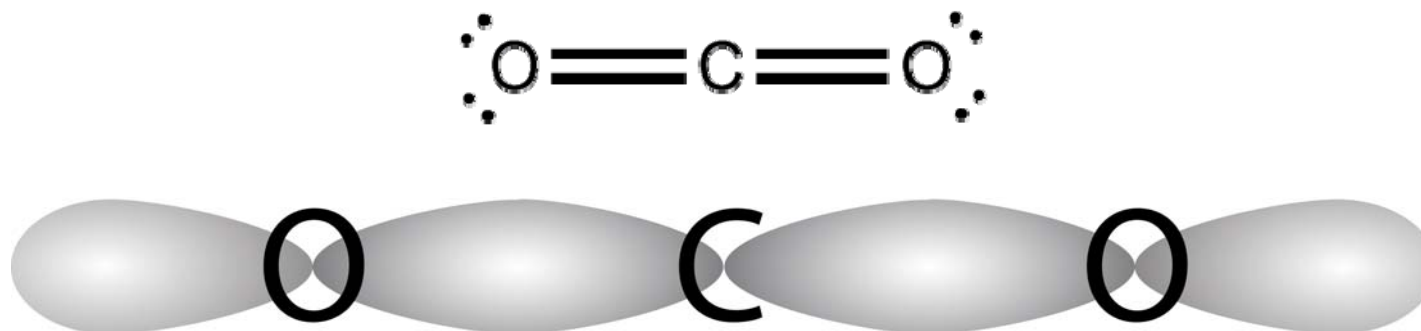
- Hybridization of **terminal atoms** the **same as their central atom**
- Terminal H **never hybridized**
- One pair in each hybrid AO  **$\sigma$  bonding MO**
- One pair in each **non-bonded hybrid AO**

## CO<sub>2</sub> sp $\sigma$ framework



sp hybrids overlap to make  
**two sp  $\sigma$  bonding MO's**,  
leaving **two sp nonbonding AO's**.  
These can hold ...

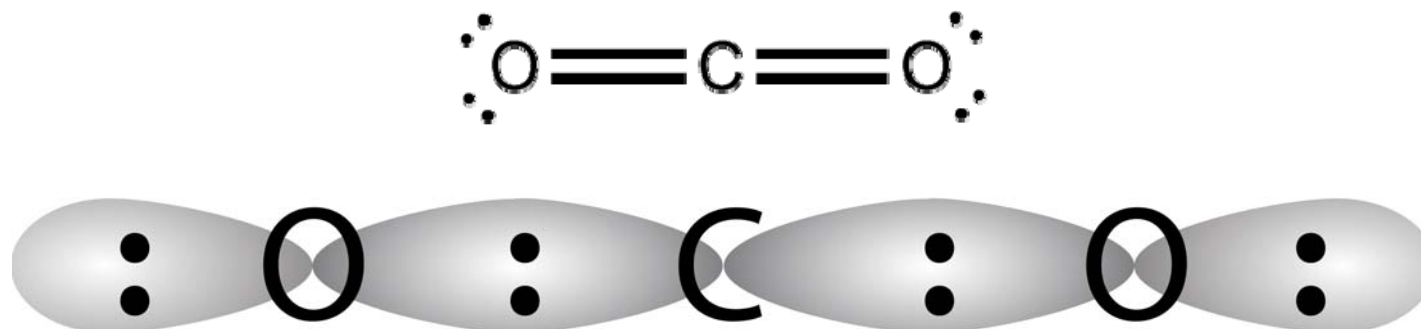
# CO<sub>2</sub> sp σ framework



sp hybrids overlap to make  
**two sp σ bonding MO's**,  
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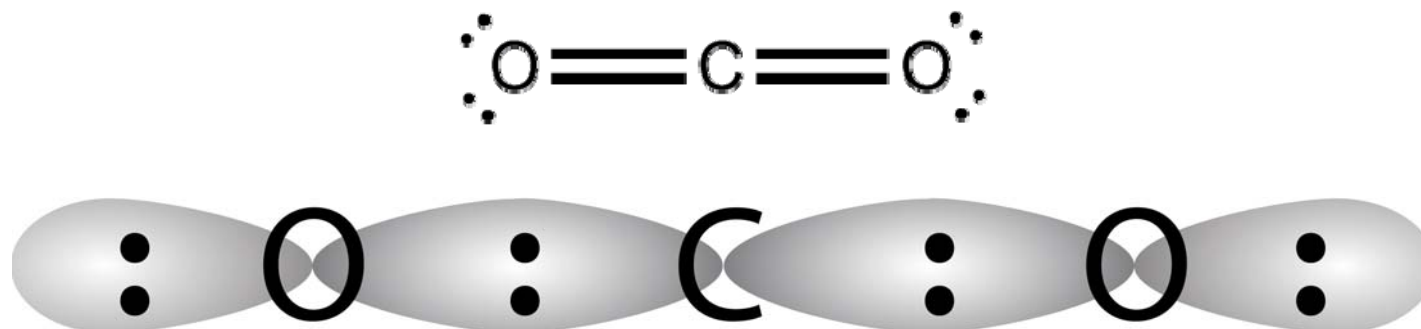


# CO<sub>2</sub> sp σ framework



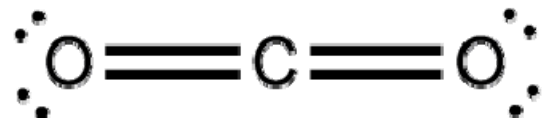
sp hybrids overlap to make  
**two sp σ bonding MO's**,  
leaving **two sp nonbonding AO's**.  
These can hold **4 pairs of electrons**.

## CO<sub>2</sub> sp σ framework



sp hybrids overlap to make  
**two sp σ bonding MO's**,  
leaving **two sp nonbonding AO's**.  
These can hold **4 pairs of electrons**.  
The remaining **4 pairs are** in the ...

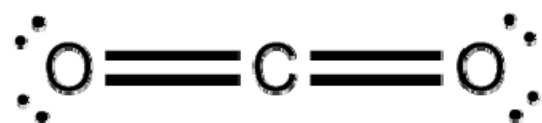
# CO<sub>2</sub> π framework



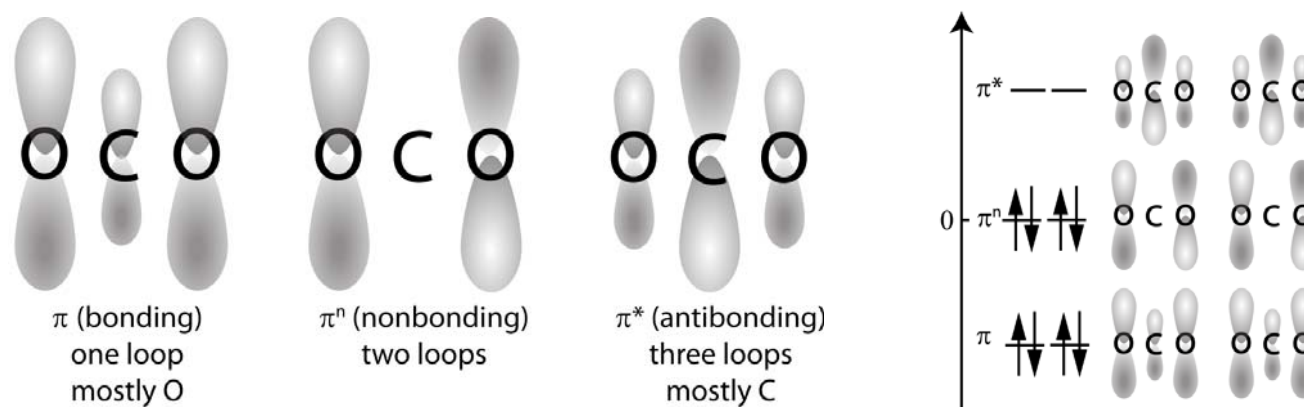
## $\pi$ framework recipe

- Unused p AO's form **same number** of  $\pi$  MO's
- **Number of loops** and **AO overlap** determine whether  $\pi$  MO is ...
  - **bonding ( $\pi$ )**
  - **nonbonding ( $\pi^n$ )**
  - **antibonding ( $\pi^*$ )**

# CO<sub>2</sub> π framework



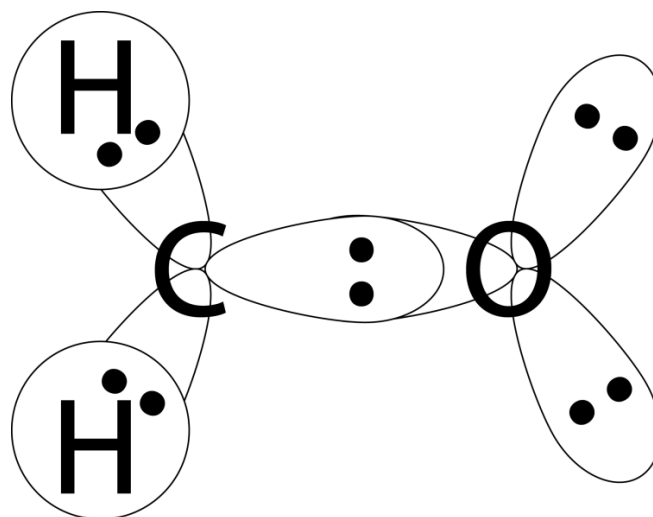
**4 pairs are** in the (**delocalized**) π framework



2 pairs in  $\pi$  (bonding) and 2 pairs in  $\pi^n$  (nonbonding); **bond order 2**

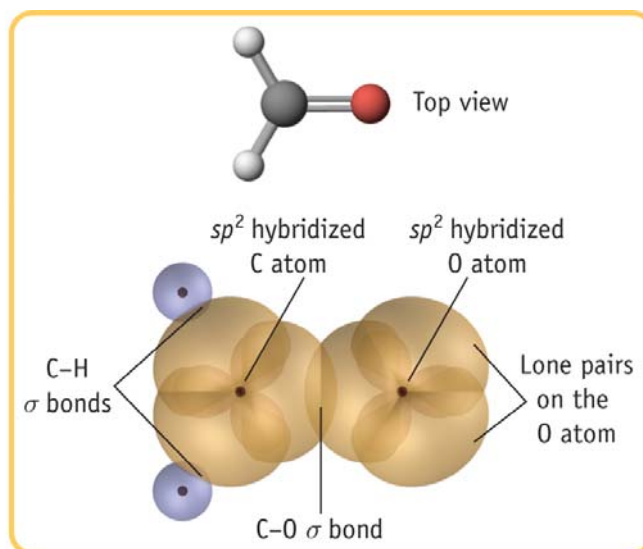
## H<sub>2</sub>CO sp<sup>2</sup> σ framework

6 pairs in Lewis structure, 5 pairs in σ framework,  
and so 1 pair in (**localized**) π framework.



# H<sub>2</sub>CO sp<sup>2</sup> σ framework

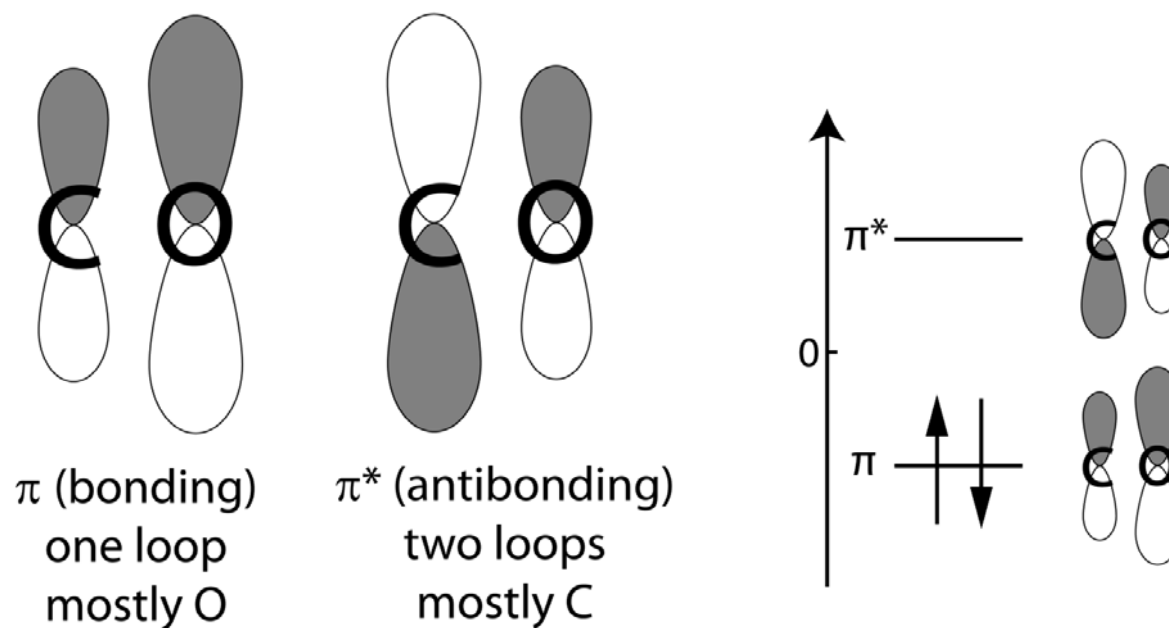
6 pairs in Lewis structure, 5 pairs in σ framework,  
and so 1 pair in (**localized**) π framework.



(b) The C-H σ bonds are formed by overlap of C atom sp<sup>2</sup> hybrid orbitals with H atom 1s orbitals. The σ bond between C and O atoms arises from overlap of sp<sup>2</sup> orbitals.

# H<sub>2</sub>CO $\pi$ framework

1 pair in (**localized**)  $\pi$  framework

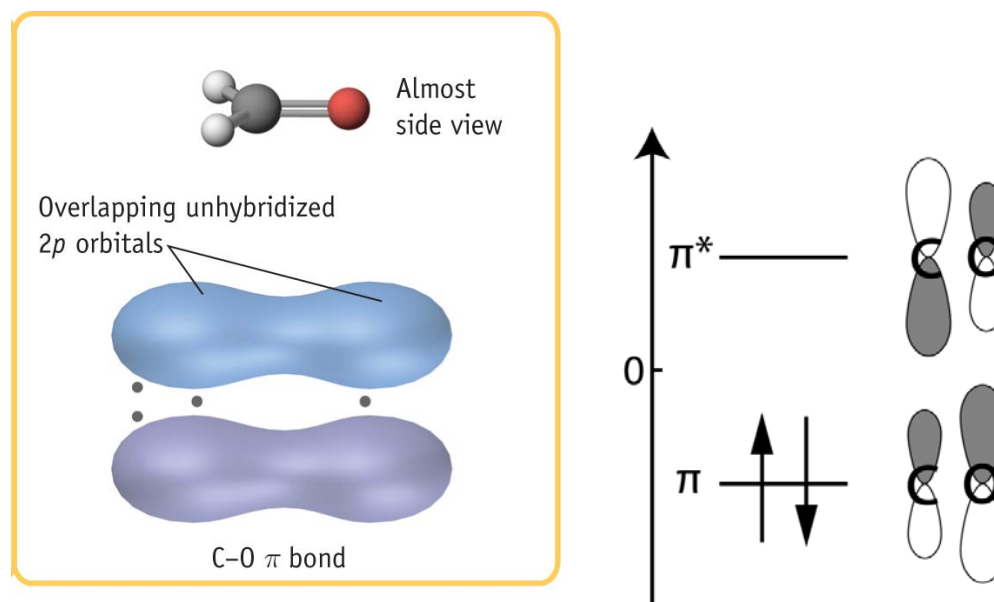


1 pair in  $\pi$  (bonding); **bond order 1**



# H<sub>2</sub>CO $\pi$ framework

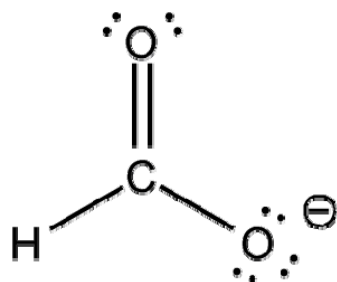
1 pair in (**localized**)  $\pi$  framework



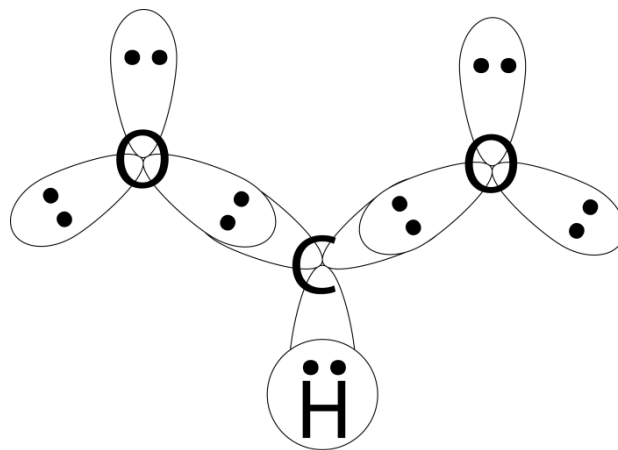
(c) The C-O  $\pi$  bond comes from the sideways overlap of  $p$  orbitals on the two atoms.

1 pair in  $\pi$  (bonding); **bond order 1**

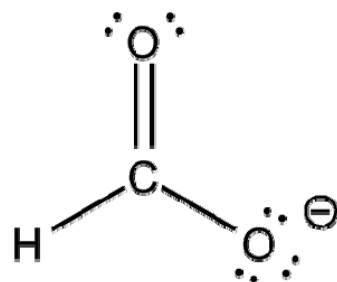
# HCOO<sup>-</sup> sp<sup>2</sup> σ framework



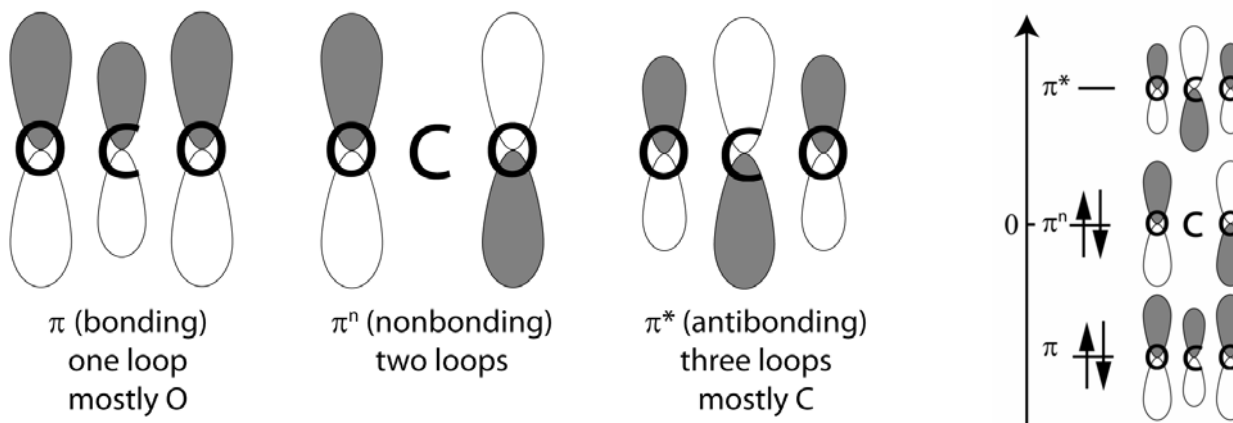
9 pairs in Lewis structure, 7 pairs in  $\sigma$  framework, and so 2 pairs in (**delocalized**)  $\pi$  framework.



# HCOO<sup>-</sup> π framework



2 pairs in (**delocalized**) π framework

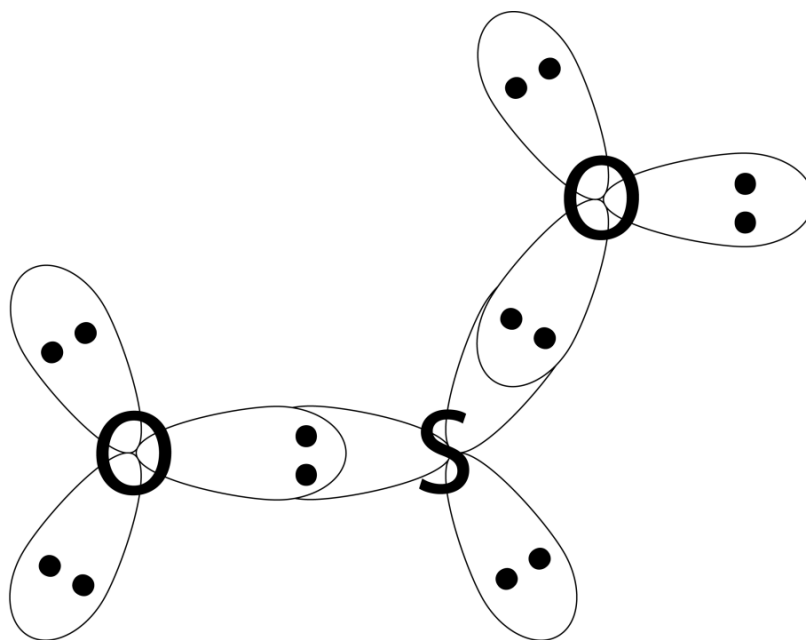


1 pair in  $\pi$  (bonding) and 1 pair in  $\pi^n$  (nonbonding);

**bond order 1**

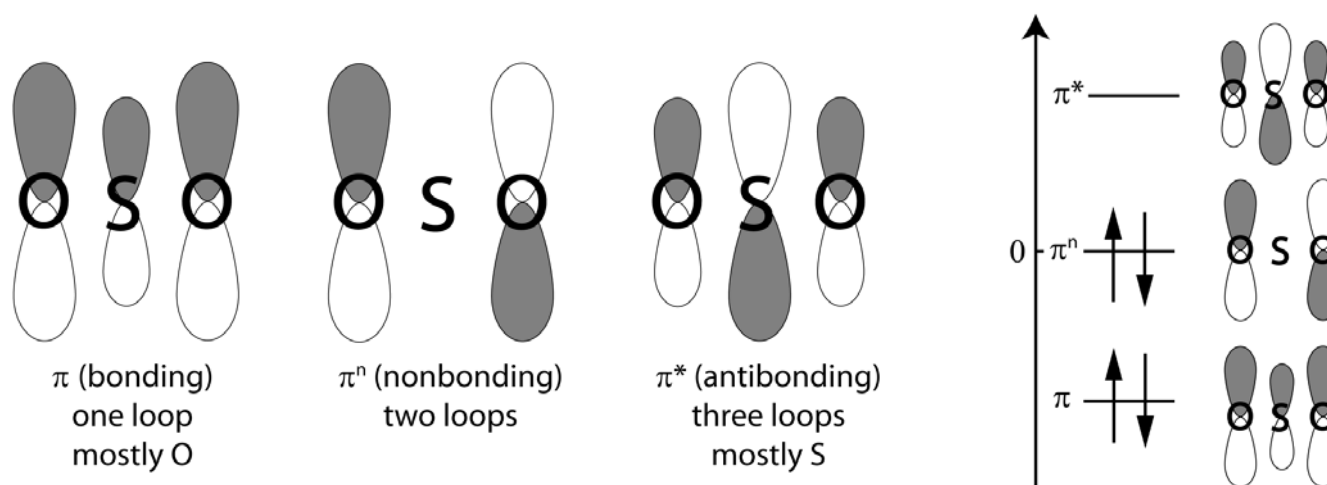
## SO<sub>2</sub> sp<sup>2</sup> σ framework

9 pairs in Lewis structure, 7 pairs in σ framework,  
and so 2 pairs in (**delocalized**) π framework.



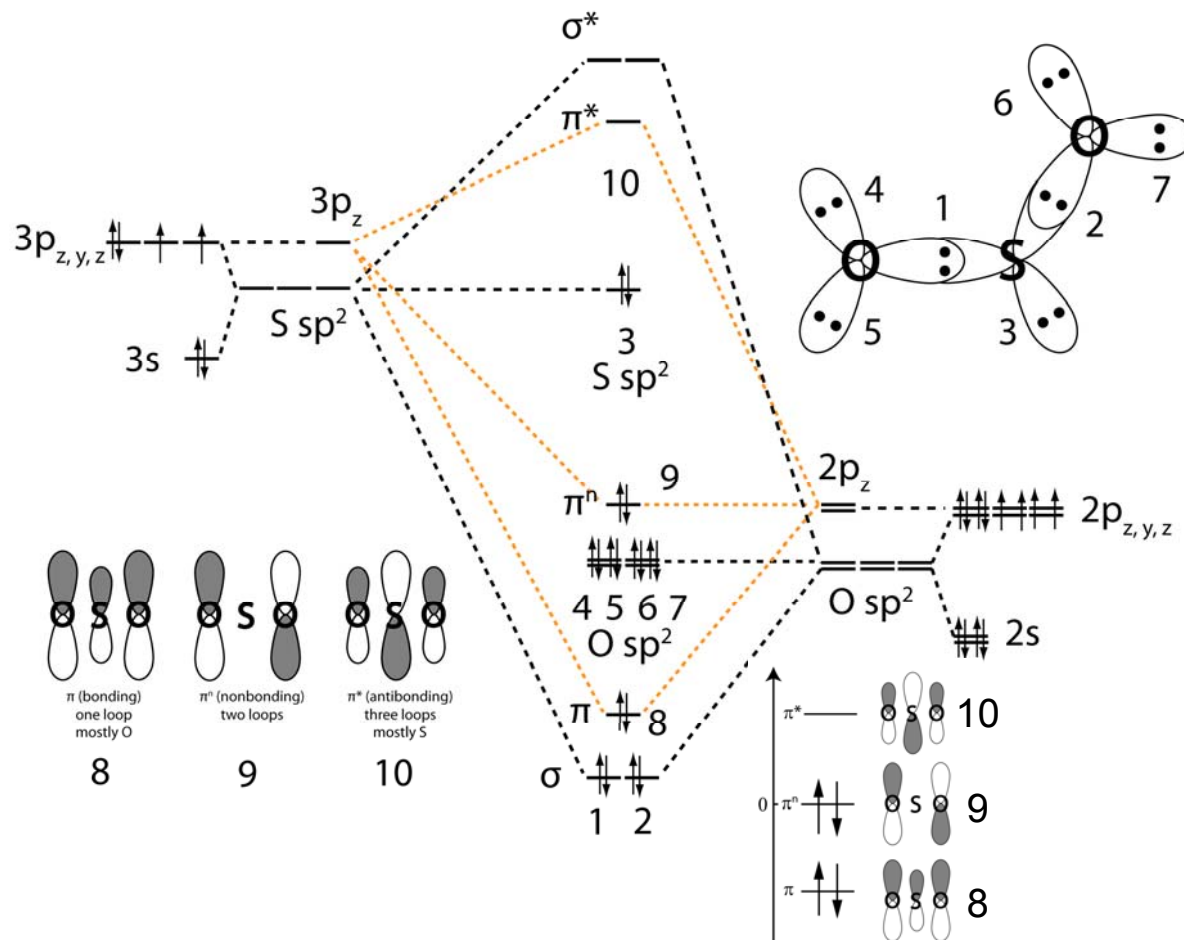
# SO<sub>2</sub> π framework

2 pairs in (**delocalized**) π framework



1 pair in  $\pi$  (bonding) and 1 pair in  $\pi^n$  (nonbonding); **bond order 1**

# SO<sub>2</sub> correlation diagram



## Do these on your own

HCOOH, formic acid

allyl:  $[\text{H}_2\text{C}=\text{CH}-\text{CH}_2]^-$ , anion;  $[\text{H}_2\text{C}=\text{CH}-\text{CH}_2]^+$ ,  
cation

$\text{H}_2\text{C}=\text{C}=\text{CH}_2$ , allene

$\text{H}_2\text{C}=\text{CH}-\text{CH}=\text{CH}_2$ , 1,3-butadiene

$\text{O}_3$ , ozone

For each one,

- Write the Lewis structure
- Sketch the  $\sigma$  framework and assign its pairs
- Sketch the  $\pi$  framework MO's, identify localization or delocalization, bonding, nonbonding, antibonding, and assign its pairs, and get the  $\pi$  bond order

## HCOOH, formic acid

Formate,  $\text{HCOO}^-$ , is planar and has

- 9 pairs
- 7 pairs in  **$\sigma$  framework**
- 1 pair in a **delocalized bonding  $\pi_1$**  orbital
- 1 pair in a **delocalized nonbonding  $\pi_2^n$**  orbital

What about formic acid?

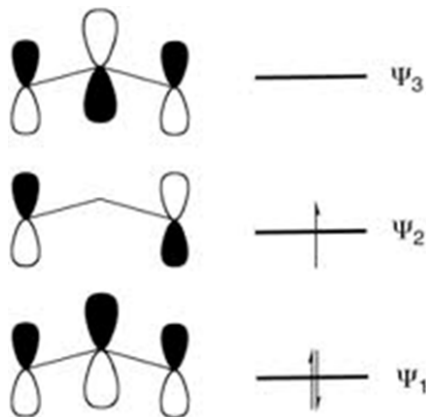
- 9 pairs
- 8 pairs in  **$\sigma$  framework**
- 1 pair in **localized bonding  $\pi_1$**  orbital



## $\text{H}_2\text{C}=\text{CH}-\text{CH}_2$ , allyl (radical)

What about allyl? Use  $-\text{CH}_2$   $\text{sp}^2$ , to have **increased delocalization**:

- 8  $\frac{1}{2}$  pairs
- 7 pairs in  **$\sigma$  framework**
- 1 pair in **delocalized bonding  $\pi_1$**  orbital
- $\frac{1}{2}$  pair (1 electron) in **delocalized nonbonding  $\pi_2^n$**  orbital



# $[\text{H}_2\text{C}=\text{CH}-\text{CH}_2]^+$ , allyl cation

What about allyl cation?

- 8 pairs
- 7 pairs in  **$\sigma$  framework**
- 1 pair in **delocalized bonding  $\pi_1$**  orbital

## $[\text{H}_2\text{C}=\text{CH}-\text{CH}_2]^-$ , allyl anion

What about allyl anion? If  $-\text{CH}_2$  is  $\text{sp}^3$ , then

- 9 pairs
- 8 pairs in  **$\sigma$  framework**
- 1 pair in **localized bonding  $\pi_1$**  orbital

If  $-\text{CH}_2$  is  $\text{sp}^2$ , then

- 7 pairs in  **$\sigma$  framework**
- 1 pair in **delocalized bonding  $\pi_1$**  orbital
- 1 pair in **delocalized nonbonding  $\pi_2^n$**  orbital

**Increased delocalization** makes  $-\text{CH}_2$  is  $\text{sp}^2$  more stable (extension to recipe)

# $\text{H}_2\text{C}=\text{C}=\text{CH}_2$ , allene

What about allene?

- 8 pairs
- 6 pairs in  **$\sigma$  framework**
- 2 pair in **two localized bonding  $\pi_1$**  orbitals

# $\text{H}_2\text{C}=\text{CH}-\text{CH}=\text{CH}_2$ , 1,3-butadiene

What about 1,3-butadiene?

- 11 pairs
- 9 pairs in  **$\sigma$  framework**
- 1 pair in **delocalized bonding  $\pi_1$**  orbital
- 1 pair in **delocalized bonding  $\pi_2$**  orbital

## O<sub>3</sub>, ozone

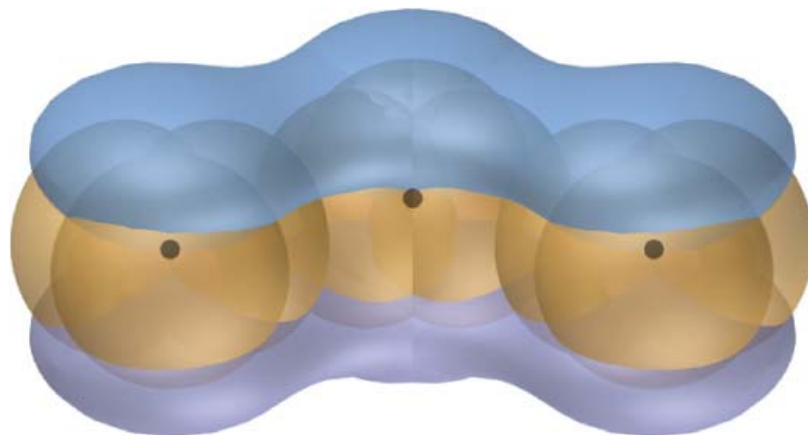
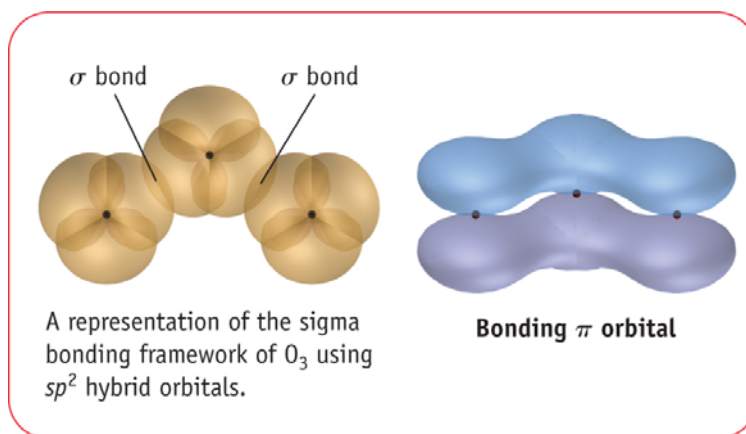
What about ozone?

- 9 pairs
- 7 pairs in  **$\sigma$  framework**
- 1 pair in **delocalized bonding  $\pi_1$**  orbital
- 1 pair in **delocalized nonbonding  $\pi_2^n$**  orbital

Ozone is polar. Why?

The two electrons in the nonbonding MO are **each only on the terminal O's!**

# O<sub>3</sub> ozone $\sigma$ and $\pi$ frameworks



$\sigma$  and  $\pi$  bonding in ozone