

Lecture 29 CH101 A1 (MWF 9 am) Fall 2016

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[TP] Atom X that has an orange emission line (650 nm) with photon energy $E_{\text{orange}} = hc/(650 \text{ nm})$ and a green emission line (510 nm) with photon energy $E_{\text{green}} = hc/(510 \text{ nm})$. Which of the following statements are true about a single emission process of atom X?

- 20% 1. An atom of X can emit light with any amount of energy.
 20% 2. An atom of X can emit light with energy between E_{orange} and E_{green} .
 20% 3. An atom of X can emit light in multiples of E_{orange} or E_{green} .
 20% 4. An atom of X can emit light only of E_{orange} or E_{green} .
 20% 5. None of the above.



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Wednesday, November 16, 2016

- Complete: Natural frequencies of atoms
- Light and matter exchange energy smoothly and slowly, <http://goo.gl/Ac4HGM>
- Light energy is exchanged in tiny amounts called photons
- Energy diagrams from light-matter resonance

Next lecture: Electron waves and quantization



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What are natural frequencies of atoms?

H atom emission spectrum



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 20% 5. None of the above.

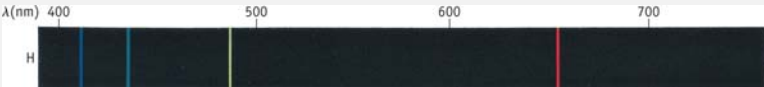


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What are natural frequencies of atoms?

H atom emission spectrum



The red light emitted has frequency 4×10^{14} Hz. IR light, due to the oscillation of protons and neutrons (nuclei), has a frequency of $\sim 1 \times 10^{13}$ Hz.

Estimate the ratio of the mass of the object oscillating in H atom that leads to the emission of visible light, relative to the mass of a proton.

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[TP] The red light emitted by H atoms has frequency 4×10^{14} Hz. The IR C-O stretch, due to the oscillation of protons and neutrons (nuclei), has a frequency of $\sim 1 \times 10^{13}$ Hz. This means that, compared to the moving mass in visible spectra, m_{atom} , the moving mass in IR spectra, m_{IR} , is

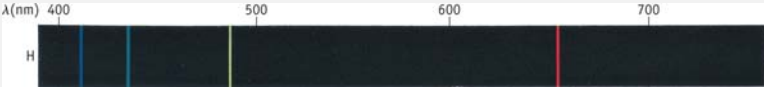
- 25% 1. ~ 15 times heavier
- 25% 2. ~ 150 times heavier
- 25% 3. $\sim 1,500$ times heavier
- 25% 4. $\sim 15,000$ times heavier

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What are natural frequencies of atoms?

H atom emission spectrum



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Estimate the ratio of the mass of the object oscillating in H atom that leads to the emission of visible light, relative to the mass of a proton.

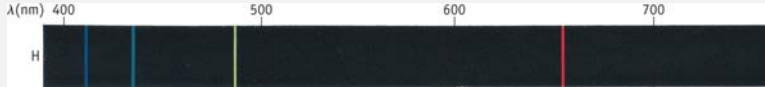
$$\nu_{\text{atom}}/\nu_{\text{IR}} \sim 40 = \sqrt{(m_{\text{IR}}/m_{\text{atom}})}$$

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What are natural frequencies of atoms?

H atom emission spectrum



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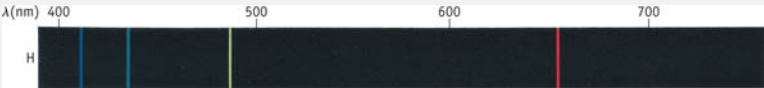
$$m_{\text{IR}}/m_{\text{atom}} \sim 40^2 \text{ so } m_{\text{IR}} \text{ is } \sim 1600 \text{ times heavier than } m_{\text{atom}}$$

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What are natural frequencies of atoms?

H atom emission spectrum



The red light emitted has frequency 4×10^{14} Hz. IR light, due to the oscillation of protons and neutrons (nuclei), has a frequency of $\sim 1 \times 10^{13}$ Hz.

Estimate the ratio of the mass of the object oscillating in H atom that leads to the emission of visible light, relative to the mass of a proton.

Motion is IR due to **atoms**, motion in atoms due to **electron clouds**.

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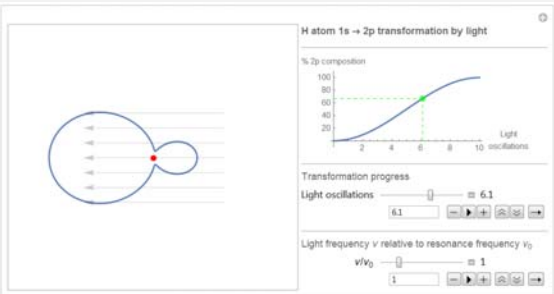
Light and matter exchange energy smoothly and slowly

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Resonant tugs by light on an electron cloud

<http://goo.gl/Ac4HGM>



H atom $1s \rightarrow 2p$ transformation by light

% 2p composition

Light oscillations

Light frequency ν relative to resonance frequency ν_0

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Non-resonant tugs by light on an electron cloud

<http://goo.gl/Ac4HGM>

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Resonant tugs by light on an electron cloud

Each oscillation takes about $1/\nu \sim 10^{-14}$ seconds

About 100,000 oscillations are required to complete the transformation

So about 10^{-9} second are required to transform the **1s cloud** into the **2p cloud**.



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Light energy is exchanged in tiny amounts called photons



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Total energy exchanged is $h \nu_{\text{light}} = h c / \lambda_{\text{light}}$

This amount energy is called a photon.



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$$\Delta E_{\text{light}} + \Delta E_{\text{atom}} = 0$$

Photon energy units are **exchanged** between light and atoms

$$\Delta E_{\text{light}} + \Delta E_{\text{atom}} = 0$$

Emission of light:

Light gains (a photon of) energy, $\Delta E_{\text{light}} = h c / \lambda$

Atom electron cloud **loses** energy, $\Delta E_{\text{atom}} = -h c / \lambda$

Absorption of light:

Light **loses** (a photon of) energy, $\Delta E_{\text{light}} = -h c / \lambda$

Atom electron cloud **gains** energy, $\Delta E_{\text{atom}} = h c / \lambda$



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$$\Delta E_{\text{light}} + \Delta E_{\text{atom}} = 0$$

Photon energy units are **exchanged** between light and atoms

$$\Delta E_{\text{light}} + \Delta E_{\text{atom}} = 0$$

Sketch the energy diagram of the atom corresponding to **emission** of **blue light**, $\lambda_{\text{blue}} = 420 \text{ nm}$.

On the same energy axis, add the energy diagram corresponding to the atom then **absorbing** of **red light**, $\lambda_{\text{red}} = 710 \text{ nm}$.



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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Why is there no emission at 600 nm?

Hint: Think about why IR absorption lines occur at particular wavenumbers?



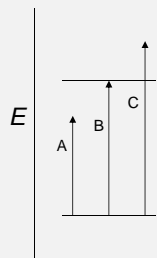
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[Quiz] On the atom energy diagram, arrows represent possible photon energies. Which arrows correspond to light **absorbed** by the atom?

- 14% 1. Only A
- 14% 2. Only B
- 14% 3. Only C
- 14% 4. Only A and B
- 14% 5. Only B and C
- 14% 6. A, B, and C
- 14% 7. None of the above



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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Lines occur only when $\nu_{\text{light}} = \nu_{\text{atom}}$, i.e., when the frequency of oscillation of the electric field of the light matches a possible natural frequency (frequency of the "jiggling") of the atom electron cloud.

Since $\nu_{\text{light}} = E_{\text{photon}} / h$ and since $E_{\text{photon}} = |\Delta E_{\text{atom}}| = |E_f - E_i| \dots$

$$\nu_{\text{atom}} = |E_f - E_i| / h$$

Therefore interaction happens only when ...

$$E_{\text{photon}} = |E_f - E_i|$$




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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Recipe to make the energy diagram that accounts for this spectrum.

1. Get lines values: 656.3 nm, 486.1 nm, 434.1 nm, and 410.2 nm.
2. Express energies in eV.

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Energy diagrams from light-matter resonance

$1 \text{ eV} = \text{energy of electron in a field of } 1 \text{ V} = 1 \text{ J/C}$

energy = charge \times voltage

$$e = 1.6021766 \times 10^{-19} \text{ C}$$

$$\text{eV} = e \times 1 \text{ J/C} = 1.6021766 \times 10^{-19} \text{ J}$$

$$E_{\text{photon}} = h \nu_{\text{light}}$$

$$= h c / (656.3 \text{ nm})$$

$$= 3.027 \times 10^{-19} \text{ J} \times \frac{1 \text{ eV}}{1.6021766 \times 10^{-19} \text{ J}}$$


$$= 1.889 \text{ eV}$$

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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Recipe to make the energy diagram that accounts for this spectrum.


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2. Express energies in eV: 1.889 eV, 2.551 eV, 2.856 eV, 3.023 eV

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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Recipe to make the energy diagram that accounts for this spectrum.


1. Lines at 656.3 nm, 486.1 nm, 434.1 nm, and 410.2 nm
2. Express energies in eV: 1.889 eV, 2.551 eV, 2.856 eV, 3.023 eV
3. Emission means **energy given off** by atom, so **downward arrows**.

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Energy diagrams from light-matter resonance

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Recipe to make the energy diagram that accounts for this spectrum.


1. Lines at 656.3 nm, 486.1 nm, 434.1 nm, and 410.2 nm
2. Express energies in eV: 1.889 eV, 2.551 eV, 2.856 eV, 3.023 eV
3. Emission means **energy given off** by atom, so **downward arrows**.
4. Assume all arrow end at **the same place**.

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Energy diagrams from light-matter resonance

The visible spectrum of hydrogen gas discharge is



Recipe to make the energy diagram that accounts for this spectrum.

Carry out this recipe at home, making diagram to scale, in your notes.

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