

Lecture 7 CH102 A1 (MWF 9:05 am) Spring 2017 Copyright © 2017 Dan Dill dan@bu.edu

[TP] The rms speed, u_{rms} , of O_2 at 25 °C is about ("Use units, Luke!") ...

25% 1. 250 m/s
 25% 2. 500 m/s
 25% 3. 750 m/s
 25% 4. 1000 m/s

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Response Counter 10 1

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 Friday, February 3, 2017

- Molecular speeds
- Distribution of molecular speeds

Next: Continue ch11: Real gases: Effect of molecular attraction; Real gases: Effect of molecular size; Real gases: van der Waals equation; phase diagrams

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Calculation of molecular speeds

$$u_{\text{avg}}^2 = 3RT/M$$

is the **fundamental connection** between microscopic **motion** and the macroscopic concept **temperature** and **molar mass**.

For a given molar mass, **higher temperature** means ...
faster moving particles.

For a given temperature, **higher mass** means ...
slower moving particles.

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Calculate rms speed of O₂ at 25 °C

$$u_{\text{avg}}^2 = 3 R T / M$$

$$u_{\text{rms}} = \sqrt{u_{\text{avg}}^2} = \sqrt{3 R T / M}$$

$R = 8.314 \text{ J}/(\text{K mol}), \text{ J} = \text{kg m}^2/\text{s}^2$

Answer: 482 m/s \approx 500 m/s



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[TP] The rms speed of O₂ at 25 °C is about 500 m/s.

Without using a calculator, use the rms speed of O₂ to estimate that the rms speed of H₂ at the same temperature is about ...

20% 1. 4000 m/s
20% 2. 2000 m/s
20% 3. 1000 m/s
20% 4. 500 m/s
20% 5. 250 m/s

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Ratio of speed of H₂ to O₂ at 25 °C


Key relation ...

$$u_1^2 / u_2^2 = M_2 / M_1$$

$$u_{\text{H}_2}^2 / u_{\text{O}_2}^2 = M_{\text{O}_2} / M_{\text{H}_2} = 32 / 2 = 16$$

$$u_{\text{H}_2} = u_{\text{O}_2} \times 4 = (500 \text{ m/s}) \times 4 = \dots$$


2000 m/s

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Distribution of molecular speeds

We have said that collisions between gas particles results in the particles having different speeds.

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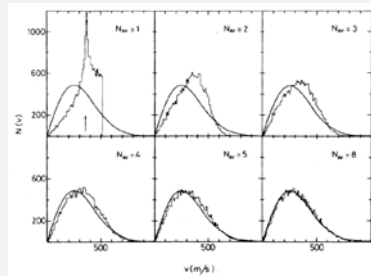
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Distribution of molecular speeds

Here is what happens to the speeds of 20,000 particles, all initially at the same speed, after they each have undergone successive numbers of collisions.

Bonomo & Riggi,
Am. J. Phys., Vol 52, p 54 (1984)
<http://dx.doi.org/10.1119/1.13809>

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Distribution of molecular speeds

The resulting distribution, known as the Maxwell-Boltzmann distribution, is always the same, depending only on temperature.

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u_{rms} versus temperature

The rms speed of H_2 at 300 K is about 2000 m/s.

Sketch the distribution of speeds of H_2 at 300 K

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u_{rms} versus temperature

Add to your sketch the distribution of speeds of O_2 at 300 K

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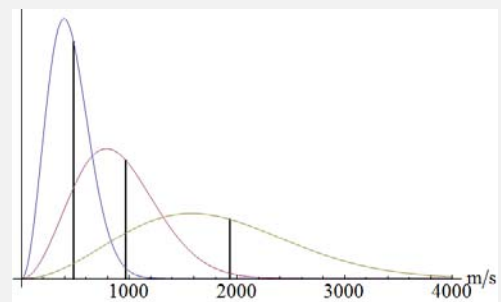
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 u_{rms} versus temperatureAdd to your sketch the distribution of speeds of O_2 at 1200 K

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 u_{rms} versus temperatureAdd to your sketch the distribution of speeds of O_2 at 1200 K

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