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[TP] An acid has $K_a = 1.0 \times 10^{-7}$ at 25 °C.
In a $c_a = 0.40$ M solution of this acid solution, $[H_3O^+] = \dots$

14% 1. 0.40
14% 2. 0.040
14% 3. 0.0010
14% 4. 0.0020
14% 5. 0.00020
14% 6. 0.00040
14% 7. Something else

BOSTON UNIVERSITY Response Counter 10 1

Lecture 19 CH102 A1 (MWF 9:05 am)
Monday, March 13, 2017

- Using K_a to get $[H_3O^+]$
- What happens when some OH^- is added to an acid?
See [Overview of acid-base calculations, https://goo.gl/GEPDqo](https://goo.gl/GEPDqo)

Next lecture: Continue: What happens when some OH^- is added to an acid?

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Using K_a to get $[H_3O^+]$

We can get the numerical value of K_a by analyzing the acid equilibrium.

	HA(aq)	$H_3O^+(aq)$	$A^-(aq)$	Q
Initial	c_a	10^{-7}	0	0
Change	$-x$	$+x$	$+x$	
Equilibrium	$c_a - x$	$10^{-7} + x$	x	K_a
Approximate	$c_a - x \approx c_a$	$10^{-7} + x \approx x$	x	K_a

Once we know K_a , we can rearrange $K_a = x^2/c_a = (10^{-pH})^2 / c_a$ to calculate the value of $x = [H_3O^+]$ for different acid molarities ...

$$x = (c_a K_a)^{1/2}$$

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Using K_a to get $[\text{H}_3\text{O}^+]$

We can get the numerical value of K_a by analyzing the acid equilibrium.

	HA(aq)	H ₃ O ⁺ (aq)	A ⁻ (aq)	Q
Initial	c_a	10^{-7}	0	0
Change	$-x$	$+x$	$+x$	
Equilibrium	$c_a - x$	$10^{-7} + x$	x	K_a
Approximate	$c_a - x \approx c_a$	$10^{-7} + x \approx x$	x	K_a

For example, if $c_a = 0.40$ and $K_a = 1.0 \times 10^{-7}$, then ...

$$x = (c_a K_a)^{1/2} = (4 \times 10^{-8})^{1/2} = 2.0 \times 10^{-4}$$



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What happens when some OH⁻ is added to an acid?



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[Quiz] An acid has $K_a = 1.0 \times 10^{-7}$ at 25 °C. The hydronium concentration of a $c_a = 0.40$ M solution of this acid solution is $[\text{H}_3\text{O}^+] = 2.0 \times 10^{-4}$. After adding some 0.20 M OH⁻, $[\text{H}_3\text{O}^+]$ must be ...

- 20% 1. smaller than 2.0×10^{-4}
- 20% 2. less than 1.0×10^{-7} (basic)
- 20% 3. equal to 1.0×10^{-7} (neutral)
- 20% 4. greater than 1.0×10^{-7} (acidic)
- 20% 5. More information needed



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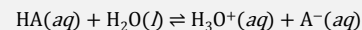
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Add "some" OH⁻ to an acid

When some OH⁻ solution is added to an HA solution, some HA will be converted to conjugate base A⁻.

Therefore, [HA] will be less, the equilibrium



will shift toward reactants, and so, by Le Chatelier, $[\text{H}_3\text{O}^+]$ must decrease.



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Add “some” OH⁻ to an acid

When some OH⁻ solution is added to an HA solution, some HA will be converted to conjugate base A⁻, and so [H₃O⁺] must **decrease**.

There are **two steps** to find the new value of [H₃O⁺].

Step 1: Assume the acid HA and the added OH⁻ react 100%, as a **limiting reagent** problem.

Step 2: Use the results of step 1 to re-solve the equilibrium.

To begin, let's learn about the **results of step 1**.



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Step 1: HA + OH⁻ limiting reagent reaction

There are three possible results of **step 1**.

“**Too little**” base: If fewer moles of OH⁻ are added than the moles of acid present, then **only some** of the acid HA will be converted to conjugate base A⁻.



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Step 1: HA + OH⁻ limiting reagent reaction

There are three possible results of **step 1**.

“**Just enough**” base: If the moles of OH⁻ added is the same as the moles of acid present, then **all** of the acid HA will be converted to conjugate base A⁻.



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Step 1: HA + OH⁻ limiting reagent reaction

There are three possible results of **step 1**.

“**Too much**” base: If the moles of OH⁻ added is more than the moles of acid present, then all of the acid HA will be converted to conjugate base A⁻ and **unused OH⁻** will be **left over**.



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[TP] $V_b = 100.$ mL of $c_b = 0.40$ M of OH^- is combined with $V_a = 100.$ mL of $c_a = 0.40$ M of HA. The result is ...

- 25% 1. "too little" OH^-
 25% 2. "just enough" OH^-
 25% 3. "too much" OH^-
 25% 4. Further information needed



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[Quiz] $V_b = 100.$ mL of $c_b = 0.20$ M of OH^- is combined with $V_a = 100.$ mL of $c_a = 0.40$ M of HA. The result is ...

- 25% 1. "too little" OH^-
 25% 2. "just enough" OH^-
 25% 3. "too much" OH^-
 25% 4. Further information needed



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[TP] $V_b = 200.$ mL of $c_b = 0.30$ M of OH^- is combined with $V_a = 200.$ mL of $c_a = 0.20$ M of HA. The result is ...

- 25% 1. "too little" OH^-
 25% 2. "just enough" OH^-
 25% 3. "too much" OH^-
 25% 4. Further information needed



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Add "some" OH^- to an acid

There are two steps to find the new value of $[\text{H}_3\text{O}^+]$.

Step 1: Assume the acid HA and the added OH^- react 100%, as a **limiting reagent problem** (ignoring equilibrium!).

Step 2: Based on whether we have added "too little", "just enough", or "too much" OH^- , we use the results of step 1 to **calculate the equilibrium** concentration of $[\text{H}_3\text{O}^+]$.




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$[\text{H}_3\text{O}^+]$ when “too little” base added

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Step 2: $[\text{H}_3\text{O}^+]$ when “too little” base added


After “too little” base is added there is present both some acid, HA, and its conjugate base, A^- . This means there are **two possible ways the system can come to equilibrium**,

$$\text{HA}(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{H}_3\text{O}^+(aq) + \text{A}^-(aq), K = K_a$$

$$\text{A}^-(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{HA}(aq) + \text{OH}^-(aq), K = K_b = K_w / K_a$$

One will result in an **acidic solution**, and the other will result in a **basic solution**.
Which one to use?

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Step 2: $[\text{H}_3\text{O}^+]$ when “too little” base added

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$$\text{HA}(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{H}_3\text{O}^+(aq) + \text{A}^-(aq), K = K_a$$


$$\text{A}^-(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{HA}(aq) + \text{OH}^-(aq), K = K_b = K_w / K_a$$

Use the one that has **the larger K !**

Say $K_a = 1.0 \times 10^{-5} \gg K_b = K_w / K_a = 10^{-14} / (1.0 \times 10^{-5}) = 1.0 \times 10^{-9}$, use ...

$$\text{HA}(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{H}_3\text{O}^+(aq) + \text{A}^-(aq), K = K_a$$

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Step 2: $[\text{H}_3\text{O}^+]$ when “too little” base added

After “too little” base is added there is present both some acid, HA, and its conjugate base, A^- . This means there are **two possible ways the system can come to equilibrium**,

$$\text{HA}(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{H}_3\text{O}^+(aq) + \text{A}^-(aq), K = K_a$$

$$\text{A}^-(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{HA}(aq) + \text{OH}^-(aq), K = K_b = K_w / K_a$$

Use the one that has **the larger K !**

Say $K_a = 1.0 \times 10^{-9} \ll K_b = K_w / K_a = 10^{-14} / (1.0 \times 10^{-9}) = 1.0 \times 10^{-5}$, use ...

$$\text{A}^-(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{HA}(aq) + \text{OH}^-(aq), K = K_b = K_w / K_a$$

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