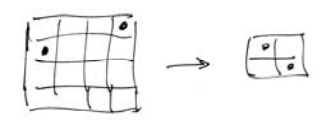


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[TP] The sketch illustrates gas  $\rightarrow$  liquid.  $\Delta S_{\text{sys}}/k_B$  for this process is ...

20% 1.  $\ln(5)$   
 20% 2.  $\ln(11)$   
 20% 3.  $\ln(1/9)$   
 20% 4. Something else.  
 20% 5. Further information needed.



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Lecture 30 CH102 A2 (MWF 11:15 am)  
 Monday, April 9, 2018

- Complete: Spontaneity of phase transitions: water  $\rightleftharpoons$  steam
- $\Delta S$  in colligative properties: Freezing point depression
- Absolute entropy

Next lecture: Entropy change of reaction. Free energy change,  $\Delta G$ .  $\Delta G$ ,  $E$ ,  $\Delta H$ ,  $\Delta S$ ,  $Q$ ,  $K$ , and  $T$ : Connection between  $T$  and  $K$ .

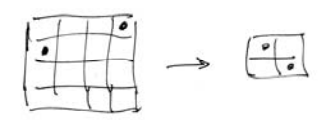
Colligative properties in terms of entropy change  
<http://quantum.bu.edu/courses/ch102-spring-2018/handouts.html>

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[TP] The sketch illustrates gas  $\rightarrow$  liquid.  $\Delta S_{\text{sys}}/k_B$  for this process is ...

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Response Counter

10 5

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steam  $\rightarrow$  water at 94 °C

Super-cooled steam at 94 °C condenses spontaneously to water.

Spontaneity means  $\Delta S_{\text{tot}} > 0$

But "gas  $\rightarrow$  liquid" means  $\Delta S_{\text{sys}} < 0$

Since condensation releases  $\Delta H_{\text{vap}}$  to the surroundings,  $\Delta S_{\text{sur}} > 0$

This means it must be  $\Delta S_{\text{sur}}$  that makes  $\Delta S_{\text{tot}} > 0$

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steam → water at 94 °C

How to get  $\Delta S_{\text{sur}}$  ?

The trick:  $\Delta S_{\text{sur}} = \Delta H_{\text{sur}}/T = -\Delta H_{\text{sys}}/T$

Hence we can always write  $\Delta S_{\text{tot}} = \Delta S_{\text{sur}} + \Delta S_{\text{sys}}$  as

$$\Delta S_{\text{tot}} = -(\Delta H_{\text{sys}}/T) + \Delta S_{\text{sys}}$$

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7

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steam → water at 94 °C

How to get  $\Delta S_{\text{sys}}$  ?

At 100 °C steam and water are in equilibrium, so ...

$$\Delta S_{\text{tot}} = 0 = +\Delta H_{\text{vap}}/(373 \text{ K}) + \Delta S_{\text{sys}}$$

From this we know that ...

$$\begin{aligned} \Delta S_{\text{sys}} &= -\Delta H_{\text{vap}}/(373 \text{ K}) \\ &= -(40.65 \times 10^3 \text{ J/mol})/(373 \text{ K}) \\ &= -108.9 \text{ J/(mol K)} \end{aligned}$$

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8

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steam → water at 94 °C

For other temperatures ...

$$\begin{aligned} \Delta S_{\text{tot}} &= -(\Delta H_{\text{sys}}/T) + \Delta S_{\text{sys}} \\ &= +(40.65 \times 10^3 \text{ J/mol})/T - 108.9 \text{ J/(mol K)} \end{aligned}$$

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9

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[TP] For steam → water

$$\Delta S_{\text{tot}} = +(40.65 \times 10^3 \text{ J/mol})/T - 108.9 \text{ J/(mol K)}$$

At  $T = 100 \text{ °C}$ ,  $\Delta S_{\text{tot}}$  evaluates to ...

0% 1. < 0

0% 2. = 0

0% 3. > 0

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Response Counter

10

10

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**[TP]** For steam  $\rightarrow$  water  

$$\Delta S_{\text{tot}} = +(40.65 \times 10^3 \text{ J/mol})/T - 108.9 \text{ J/(mol K)}$$
 At  $T = 106 \text{ }^\circ\text{C}$ ,  $\Delta S_{\text{tot}}$  evaluates to ...

0% 1.  $< 0$   
 0% 2.  $= 0$   
 0% 3.  $> 0$

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Response Counter

10

12

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## Taking stock

Spontaneity **means** that ...  

$$\Delta S_{\text{tot}} = \Delta S_{\text{sys}} + \Delta S_{\text{sur}} > 0$$

Spontaneity **does not** require that ...  

$$\Delta S_{\text{sys}} > 0 \text{ or } \Delta S_{\text{sur}} > 0$$

The **separate roles** of  $\Delta S_{\text{sys}}$  and  $\Delta S_{\text{sur}}$  account for why **steam condenses** and **water boils**

The same approach works for **melting** and for **sublimation**

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The role of  $\Delta S$  in colligative properties

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16

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## $\Delta S$ and freezing point depression

Make a diagram of  $S$  (vertical axis) for liquid and solid water (ice).  
 Connect the two entropies with an arrow corresponding to liquid  $\rightarrow$  solid.  
 What is the length of the arrow?

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17

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## $\Delta S$ and freezing point depression

How is  $S(\text{liquid})$  changed by adding a small amount of solute?

What must happen to the length of the arrow connecting the water solution to pure ice?

How can this change come about?

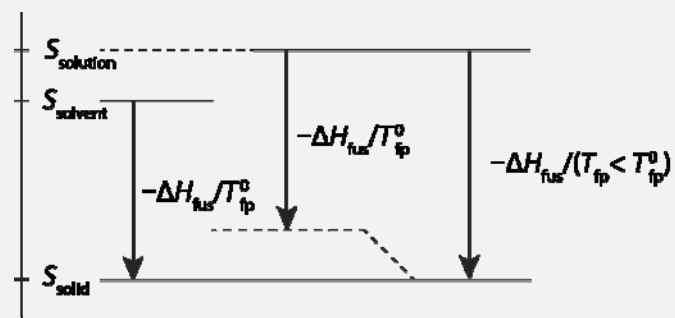


18

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## $\Delta S$ and freezing point depression



19

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## $\Delta S$ and colligative properties

Each of the four colligative properties can be understood in terms of entropy changes.

See the notes on colligative properties at ...

<http://quantum.bu.edu/courses/ch102-spring-2018/handouts.html>



20

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Absolute entropy,  $S^\circ$ : The third law of thermodynamics



21

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## How to determine $\Delta S_{\text{sys}}$ for a chemical reaction?

We have seen that we can get  $\Delta S_{\text{sys}}$  for a **phase transition** using  $\Delta S_{\text{tot}} = 0$  at the transition temperature.

$$\Delta S_{\text{sys}} = \Delta H_{\text{sys}} / T_{\text{transition}}$$



22

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## How to determine $\Delta S_{\text{sys}}$ for a chemical reaction?

Getting  $\Delta S_{\text{sys}}$  for a **chemical reaction** requires a different approach.

In principle we could get  $\Delta S_{\text{sys}}$  by analyzing changes in particle and energy dispersal due to the reaction.

But, in practice, it is easier to get  $\Delta S_{\text{sys}}$  by measuring heat flow between system and surroundings when they are in equilibrium.



23

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## How to determine $\Delta_r S^\circ$ ?

At 0 K, for each substance,  $W = 1$  and so  $S = 0$ .

This is known as the **third law of thermodynamics**.

Starting for  $S(\text{at } T = 0) = 0$ , adding a little heat  $dq$ , entropy  $dS = dq / \sim 0K$  will be added, raising  $T$  a little bit, say to 1 K.

Adding a little more heat  $dq$ , entropy  $dS = dq / \sim 1K$  will be added, raising  $T$  a little bit, say to 2 K.

Continuing in this way, up to a final temperature  $T$ , the sum of all of the small additions  $dS$  are  $S$  for the substance at  $T$ .

These values  $S$  are called **absolute entropies**.



24