

## Half-life example calculations

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Boston University

## Half-life calculations

Fundamental relation

$$(1/2)^n N_0 = N$$

1. Half life is  $n$  for  $N/N_0 = 1/2$ ; independent of  $N_0$ .
2. Given  $N/N_0$  after time  $t$ , calculate  $n$ , and then  $t_{\text{half}} = t/n$
3. Given  $n$ , calculate  $N/N_0$ , the fraction remaining after  $t = n t_{\text{half}}$

## Half-life calculations

$$(1/2)^n N_0 = N$$

Half-life is 33 minutes. **What fraction remains** after 75 minutes?

Strategy: Use  $n = 75/33$  and then fraction remaining =  $N/N_0 = (1/2)^n$

Answer:  $n = 75/33 = 2.3$ ,  $(1/2)^n = \mathbf{0.21 (21\%)}$

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$$(1/2)^n N_0 = N$$

Half-life is 11 days. **How long to decay** by 10%?

Strategy: Use  $N/N_0 = 0.90$ , solve  $N/N_0 = (1/2)^n$  for  $n = \text{time}/t_{\text{half}}$ , and so  $\text{time} = n \times t_{\text{half}}$

Answer:  $\log[(1/2)^n] = -n \log(2) = \log(N/N_0)$   
so  $n = -\log(N/N_0)/\log(2)$   
 $= -\log(0.90)/\log(2) = 0.152$ ,  
hence,  $\text{time} = 0.152 \times 11 \text{ days} = \mathbf{1.7 \text{ days}}$

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$$(1/2)^n N_0 = N$$

A sample decays by 25% in 15 minutes. **What is its half-life?**

Strategy: Use  $N/N_0 = 0.75$  and  $n = 15 \text{ min}/t_{\text{half}}$ , solve  $N/N_0 = (1/2)^n$  for  $n = \text{time}/t_{\text{half}}$ , and so  $t_{\text{half}} = \text{time}/n$

Answer:  $n = -\log(N/N_0)/\log(2)$   
 $= -\log(0.75)/\log(2) = 0.415$ ,  
hence  $t_{\text{half}} = 15/0.415 \text{ minutes} = \mathbf{36 \text{ minutes}}$

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CPS lesson: Half-life examples